Design And Implementation Of PFC CUK Converter-Based PMBLDCM Drive

S. Kaliappan*, R. Thenmozhi**
*(Assistant Professor, Department of Electrical and Electronics Engineering, Kumaraguru College of Technology, Coimbatore-46)
**(Student, M.E- Powe Electronics, Kumaraguru College of Technology, Coimbatore-46)

ABSTRACT
This method is used to improve the efficiency of motor drive by power factor correction. It plays an important role in energy saving during energy conversion. A cuk dc–dc converter topology reduced the power quality problems and improve the power factor at input ac mains. A three-phase voltage-source inverter is used as an electronic commutator operates the PMBLDCM drive. The concept of voltage control at the dc link proportional to the desired speed of the PMBLDCM is used to control the speed of the compressor. The proposed power factor converter topology is designed, modeled, and its performance is evaluated in matlab-simulink environment. The results show an improved power quality and good power factor in wide speed range of the drive. It also compares the Total Harmonic Distortion (THD) of the Input AC current with PID controller in Matlab-Simulink environment.

Keywords – Cuk converter, Diode Bridge Rectifier (DBR), Permanent magnet brushless dc motor (PMBLDCM), Power factor correction (PFC), Voltage-source inverter (VSI).

I. Introduction
Permanent magnet brushless dc motor is used for low power applications. The commutation in a PMBLDCM is done by solid state switches of a three phase voltage source Inverter (VSI). If air-conditioning (Air-Con) system operated under speed control results in an improved efficiency of the system. PMBLDCM has reduced electrical and mechanical stresses, low running cost, long life compared to a single phase induction motor.[1] [2] [3] A PMBLDCM has developed torque proportional to its phase current and its back electromotive force (EMF), which is proportional to the speed. Therefore, a constant torque is maintained in its stator windings. VSI is used for electronic commutation based on the rotor position signals of the PMBLDC motor. The PMBLDCM drive is fed from a single phase ac supply through a diode bridge rectifier (DBR) followed by a capacitor at dc link. Due to an uncontrolled charging of the capacitor at dc link, draws a pulsed current.

With a peak higher than the amplitude of the fundamental input current at ac mains. This results in poor power quality (PQ) at ac mains in terms of poor power factor (PF), high total harmonic distortion (THD) and high crest factor (CF). Therefore, for PMBLDCM a PF correction (PFC) converter among various available converter topologies is used.

The Cuk dc–dc converter is used as a PFC Converter. The main advantages of using a Cuk dc–dc converter compared to other single switch converters are: continuous input and output currents, small output filter, wide output voltage range, almost near unity power factor with simple control and small size.

II. Proposed speed control scheme of PMBLDC motor
Figure.1 shows the proposed speed control scheme is based on the control of the dc link voltage reference as a comparable to the reference speed. The rotor position signals established by Hall-effect sensors.
sensors are used by an electronic commutator to generate switching sequence for the VSI which in turns feeds the PMBLDC motor. Therefore, rotor position is necessary only at the commutation point. The dc link voltage is controlled by Cuk dc-dc converter by making use of capacitive energy transfer which result is non-pulsating input and output currents. The suggested PFC converter is operated in high switching frequency for fast and effective control. It uses metal-dioxide semiconductor field effect transistor (MOSFET) for high-frequency operation.

A current multiplier is used in PFC control scheme with a current control loop within the speed control loop for continuous-conduction-mode operation. By comparing sensed dc link voltage \( V_{\text{dc}} \) and a voltage \( V_{\text{dc}'} \) equivalent to the reference speed, voltage error \( V_r \) is obtained. The control loop begins with the processing of voltage error \( V_r \), through a proportional (PID) controller to give the modulating control signal \( I_c \). The reference dc current \( I_{d\text{c}} \) is obtained multiplying signal \( I_c \) with a unit template of input ac voltage. It is then compared with the dc current \( I_{d\text{c}} \) sensed after the DCR. The resultant current error \( I_e \) is amplified and compared with the saw tooth carrier wave of fixed frequency \( f_s \) to generate the pulse width modulation (PWM) pulse for the Cuk converter. Its duty ratio \( D \) controls the dc link voltage at the desired value.

### III. PFC cuk converter design

In the proposed framework, the PFC Cuk converter is designed for a PMBLDCM with main considerations on the PQ improvement at ac mains and speed control of the Air-Conditioner. DC link voltage of the PFC converter is given by the following equation:[4] [5] [6]

\[
V_d = \frac{V_{\text{avg}}}{1-D}
\]

(1)

Where \( V_{\text{avg}} \) is the average output of the DBR for a given ac input voltage \( V_{\text{ac}} \) related as,

\[
V_{\text{avg}} = \frac{2\sqrt{2}}{\pi} V_s
\]

(2)

The Cuk converter uses inductor \( L_i \) and capacitor \( C \) for energy transfer. Their values are given by,

\[
L_i = \frac{D V_{\text{avg}}}{f_s (\Delta L_{ii})}
\]

(3)

\[
C = \frac{D I_{d\text{c}}}{f_s \Delta V_C}
\]

(4)

Where \( \Delta L_{ii} \) is inductor current ripple, \( \Delta V_C \) is voltage ripple in the capacitor \( C \), and the current drawn by PMBLDCM is denoted by \( I_{d\text{c}} \).

A ripple filter is designed for ripple-free voltage. The inductance \( L \) of the ripple filter limits the inductor peak-to-peak ripple current \( (\Delta I_{il}) \) within a specified value for the given switching frequency \( f_s \), whereas the capacitance \( C_{dc} \) is calculated for the allowed ripple in the dc link voltage \( (\Delta V_{dc}) \). The values of the ripple filter inductor and capacitor are given as,

\[
L = \frac{(1-D) V_{\text{dc}}}{f_s (\Delta I_{il})}
\]

(5)

\[
C = \frac{I_{d\text{c}}}{2\omega (\Delta V_{dc})}
\]

(6)

### IV. Modeling of PFC converter-based PMBLDCM drive

The main components of proposed drives are PFC converter and PMBLDCM. They are modeled using mathematical equations. Then the complete model of the drive is obtained by combining the individual models.

#### 4.1. PFC converter

The modeling of a PFC converter consists of modeling of the voltage controller, reference current generator and a PWM controller.

##### 4.1.1. Voltage controller:

The modeling of a voltage controller is important since the performance of the PMBLDCM drive depends on this controller. The proportional integral derivative (PID) controller is used to control the DC link voltage. If, at the \( k_a \) instant of time, \( V^*_{dc}(k) \) is the reference dc link voltage and \( V_d(k) \) is the voltage sensed at the dc link, the voltage error \( V_r(k) \) is then given by:

\[
V_r(k) = V^*_{dc}(k) - V_d(k)
\]

(7)

##### 4.1.2. Reference current generator:

The reference current \( i^*_{dc} \) is

\[
i^*_{dc} = I_{c}(k)v_{u}, V_s
\]

(8)

Where \( u, v_s \) is the unit template of the ac mains voltage, calculated as

\[
u_s = \frac{v_s}{\sqrt{2}},
\]

(9)

\[
u_s = v_{sm} \sin \omega t.
\]

(10)

\[
u_s = v_{sm} \sin \omega t.
\]

(11)

where frequency \( \omega \) is in radians per second and amplitude \( v_{sm} \) is in volts.

##### 4.1.3. PWM controller:

The reference current of the Cuk converter \( i^*_{dc} \) is compared with its current \( I_{dc} \) to generate the current error,

\[
\Delta I_{dc} = (i^*_{dc} - I_{dc})
\]

(12)

The switching signals of the MOSFET in the PFC converter are produced by relating amplified current error by gain \( k_i \) with fixed frequency \( f_s \) of the saw tooth carrier waveform \( m(t) \)

If \( k_i \Delta I_{dc} > m(t) \) then \( S = 1 \ else S = 0 \)

(13)

where \( S \) is the switch of the MOSFET in Cuk converter. Its values “1” and “0” represent “on” and “off” conditions, respectively.

#### 4.2. PMBLDCM

The PMBLDCM motor can be modeled using differential equations given by, [7] [8] [9]

\[
\dot{v}_{xy} = R_{ix} + \omega \lambda_x + e_{xn}
\]

(14)

\[
v_{yn} = R_{iy} + \omega \lambda_y + e_{yn}
\]

(15)

\[
v_{zn} = R_{iz} + \omega \lambda_z + e_{zn}
\]

(16)

where \( d \) is the differential operator \( (d/dt) \), \( i_x, i_y, \) and \( i_z \) are currents, \( \lambda_x, \lambda_y, \) and \( \lambda_z \) are flux linkages, and \( e_{xn}, e_{yn}, \) and \( e_{zn} \) are phase-to-neutral back EMFs of
PMBLDCM, in particular phases; R is the resistance of motor windings/phase. The flux linkages can be denoted as,
\[ \lambda_x = L_s i_x - M (y_x + i_z) \]  \hspace{1cm} (17)
\[ \lambda_y = L_s i_y - M (x + i_z) \]  \hspace{1cm} (18)
\[ \lambda_z = L_s i_z - M (y + i_x) \]  \hspace{1cm} (19)
where self-inductance/phase is Ls and mutual inductance is M. The developed torque Te is given by,
\[ T_e = (e_{an} + e_{cn})/2 \]  \hspace{1cm} (20)
Then PMBLDCM has no neutral connection
\[ i_x + i_y + i_z = 0 \]  \hspace{1cm} (21)
From (14)–(19) and (21), the voltage between the neutral point and midpoint of the dc link is given by,
\[ v_{no} = \{ v_{no} + v_{yo} + v_{zo} - (e_{an} + e_{bn} + e_{cn}) \}/3 \]  \hspace{1cm} (22)
From (15)–(17) and (19), the flux linkages are given by,
\[ \lambda_x = (L_s + M) i_x, \lambda_y = (L_s + M) i_y, \lambda_z = (L_s + M) i_z. \]  \hspace{1cm} (23)
From (17)–(19) and (23), the current derivatives in generalized state-space form are given by,
\[ \frac{di_x}{dt} = (v_{an} - i_x R - e_{an})/(L_s + M) \]  \hspace{1cm} (24)
where a represents phase x, y, or z.
The back EMF is a function of rotor position (θ) as
\[ e_{an} = K_b \sin(\theta) \]  \hspace{1cm} (25)
where a can be phase x, y or z and consequently fa (θ) denotes function of rotor position with a maximum value ±1, equal to trapezoidal induced emf given by,
\[ f_x(\theta) = 1 \text{ for } 0 < \theta < 2\pi/3 \]  \hspace{1cm} (26)
\[ f_x(\theta) = 1\{(6/\pi)(\pi - \theta)\} - 1 \text{ for } 2\pi/3 < \theta < \pi \]  \hspace{1cm} (27)
\[ f_x(\theta) = -1 \text{ for } \pi < \theta < 5\pi/3 \]  \hspace{1cm} (28)
\[ f_x(\theta) = 1\{(6/\pi)(\pi - \theta)\} + 1 \text{ for } 5\pi/3 < \theta < 2\pi. \]  \hspace{1cm} (29)
The functions fy(θ) and fz(θ) are similar to fx(θ) with phase differences of 120° and 240°, respectively. Therefore, the electromagnetic torque expressed as,
\[ T_e = K_b \{ f_x(\theta)i_x + f_y(\theta)i_y + f_z(\theta)i_z \}. \]  \hspace{1cm} (30)
The mechanical equation of motion in speed derived form is given by,
\[ \frac{d\omega}{dt} = (P/2)(Te - T_l - B\omega)/(J) \]  \hspace{1cm} (31)
where derived of rotor position \[ \dot{\theta} \] is wr. number of poles is P, load torque in newton meters is Tl, moment of inertia in kilogram square meters is J, and friction coefficient is B in newton meter seconds per radian.
The derivative of rotor position is given by,
\[ \dot{\theta} = \omega \]  \hspace{1cm} (32)
Equations (14)–(32) represent the dynamic model of the PMBLDC motor.

V. Matlab/Simulink modeling and simulation results

Proposed cuk converter using Conventional PID controller.

Fig.2: Matlab/Simulink model of proposed cuk converter using conventional PID controller.

Fig.3a: Current waveform across the source

Fig.3b: Voltage and current waveform across the source

Fig.3c: Back emf of the PMBLDC motor drive.
VI. Conclusion

A new speed control scheme for a PMBLDCM using PID CONTROLLER in the control circuit has been simulated for an air-conditioner using a Cuk PFC converter. The speed of PMBLDCM has been found to be proportional to the dc link voltage; so, a smooth speed control is observed while controlling the dc link. The PFC Cuk converter gives near unity power factor in a wide range of the speed and the input ac voltage. Various power quality problems like poor power factor, inrush current, and speed control may be can be resolved by the proposed voltage-controlled PFC Cuk converter-base PMBLDCMD.

References


[8]. A Voltage-Controlled PFC Cuk Converter-Based PMBLDCM Drive for Air-Conditioners Sanjeev Singh, Member, IEEE, and Bhim Singh, Fellow, IEEE.

Authors Biography

Mr. S. Kaliappan, completed his Diploma in Electronics and Communication from Kongu Polytechnic, Coimbatore, Tamil Nadu and obtained his B.E degree in the department of Electrical and Electronics Engineering from Government College of Technology, Coimbatore, Tamil Nadu and obtained his M.E degree in the specialization of Embedded System in Anna University of Technology, Coimbatore, Tamil Nadu. His areas of interests are Power Systems and Embedded Systems. He has published six papers in National Conferences and four papers in International Conferences.

R. THENMOZHI completed her B.E(EEE) in Kongu Engineering College 2012, Erode, and pursuing final year M.E. in Power Electronics and Drives in Kumaraguru College of Technology, Coimbatore. Her area of interest is Power Electronics. She has presented a paper in international conference.