V.U.K. Sastry, K. Anup Kumar / International Journal of Engineering Research and Applications (IJERA) ISSN: 2248-9622 www.ijera.com Vol. 2, Issue 5, September- October 2012, pp.951-958 A Block Cipher Obtained By Blending Modified Feistel Cipher And Advanced Hill Cipher Involving A Single Key Matrix

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Abstract

In this investigation, we have developed a block cipher which includes the basic ideas of the modified Feistel cipher and the advanced Hill cipher. In the advanced Hill cipher, as the modular arithmetic inverse of a matrix is the same as the matrix itself, the computations involved in the development of the inverse of the matrix are reduced remarkably. The cryptanalysis carried out in this investigation clearly shows that the strength of the cipher is quite significant as the system of equations occurring in the encryption process are nonlinear, and the supporting functions such as Shift () and Mix () are causing confusion and diffusion in each round of the iteration process.

Key words: Encryption, Decryption, Key matrix, Shift, Mix, XOR Operation.

1. Introduction

In the recent investigations [1-8], we have developed several block ciphers by generalizing the classical Feistel cipher wherein we have considered a plaintext which can be represented in the form of a pair of matrices instead of a pair of binary strings that was used in the case of classical Feistel cipher.

In this development, we have used a key on both the sides of a portion of the plaintext matrix, and made use of iteration. In the iteration process, we have included the features, namely, mixing, permutation, and XOR operation, blending and shuffling. In this, we have seen that the strength of the cipher enhances quite significantly as all the three features, involved in the iteration process thoroughly modify the plaintext before it becomes the cipher text. The avalanche effect and the cryptanalysis discussed in this analysis effectively indicate that the cipher is a strong one.

In a recent investigation, Bibhudenra Acharya et al. [9] have developed Advanced Hill Cipher using an involutory matrix. In the present paper, our objective is to develop the modified Feistel cipher using the features of Advanced Hill cipher. The basic equations governing the encryption and the decryption of this cipher are given by

$P_i = (K Q_{i-1} K) \mod N$)	(1.1)
$Q_i = P_{i-1} \bigoplus P_i$ and	Ţ	i = 1 to n .
$\mathbf{Q}_{i-1} = (\mathbf{K} \mathbf{P}_i \mathbf{K}) \mod \mathbf{N}_i$	Í	(1.2)
$P_{i-1} = Q_i \oplus P_i$	}	i = n to 1.

where, P_i and Q_i are the plaintext matrices at the ith stage of the iteration, K the involutory key matrix and N is a positive integer chosen appropriately. Here n denotes the number of iterations. In the development of this cipher, we have utilized the functions Mix () and Shift (), and XOR operation.

In what follows, we present the plan of the paper. In section 2, we discuss the development of the involutory matrix. In section 3, we discuss the development of the cipher and present the flowcharts and the algorithms describing the cipher. Section 4 is devoted to an illustration of the cipher, and in this we have determined the avalanche effect. We have examined the cryptanalysis in section 5. Finally in section 6, we have given the details of the computations and arrived at the conclusions.

2. Development of the Involutory Matrix

An involutory matrix is a square matrix whose inverse is same as the original matrix.

Let $A = [a_{ij}]$ be a square matrix of size n. Let it be denoted as

$$A = \begin{bmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{bmatrix}$$
(2.1)

Where all the sub matrices A_{11} , A_{12} , A_{21} and A_{22} are square matrices of size n/2.

As the modular arithmetic inverse of an involutory matrix is governed by the relations

$$(A A^{-1}) \mod N = I,$$
 (2.2)

and	$\mathbf{A} = \mathbf{A}^{-1}$	(2.3)
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Thus we have, $A^2 \mod N = I$ (2.4)

Here I is an identity matrix and N is any non zero positive integer chosen appropriately.

From (2.1) and (2.4) we get,

$A_{22} \bmod N = -A_{11} \bmod N,$	(2.5)	
$A_{12} = [d (I - A_{11})] \mod N$	(2.6)	
$A_{21} = [w(I + A_{11})] \mod N$	(2.7)	
where (dw) mod $N = 1$	(2.8)	

Given A_{11} , on selecting d, where d lies in the interval 0 < d < N, firstly we obtain w from (2.8), then we determine A_{22} , A_{12} and A_{21} by satisfying the relations (2.5) to (2.7).

If A_{11} is the key, a square matrix of size n/2, then we get the involutory matrix A of size n.

1. Development of the Cipher

Consider a plaintext P consisting of $2m^2$ characters. On employing the EBCIDIC code, the plaintext can be written in the form of a pair of square matrices P₀ and Q₀, wherein, each one is of size m. Let us consider a key matrix K, whose size is mxm.

In this cipher, the encryption and the decryption are governed by the relations (1.1) and (1.2) respectively. In what follows we present the flow charts and the algorithms describing the encryption and the decryption processes.





Fig 1. The process of Encryption

In the matrices P_i and Q_i , all the numbers are lying in the interval [0-255]. Here K is the involutory matrix of the key matrix, in this analysis, we have taken n = 16.

In the flowchart, for the sake of elegance, we have written the functions Mix() and Shift(), arising in encryption, as M() and S()respectively. The reverse processes represented by IMix() and IShift(), arising in decryption, are denoted by IM() and IS().



Fig 2. The process of Decryption

The processes of encryption and decryption depicted in the flow charts are described by the algorithms given below.

Algorithm for Encryption

1.Read P, A, n and N. 2.K = Involute (A) 3. P_0 = Left half of P. Q_0 = Right half of P. 4. for i = 1 to n begin $P_i = (K Q_{i-1} K) \mod N$ $Q_i = P_{i-1} \bigoplus P_i$ $P_i = M (P_i)$ $P_i = S (P_i)$ $Q_i = M (Q_i)$ $Q_i = S (Q_i)$ end 5. $C = P_n ||Q_n /*||$ represents concatenation */ 6. Write(C)

Algorithm for Decryption

1.Read C, A, n and N. 2.K = Involute (A) 3. P_n = Left half of C Q_n = Right half of C 4. for i = n to 1 begin P_i = IS (P_i) P_i = IM (P_i) Q_i = IS (Q_i) Q_i = IS (Q_i) Q_{i-1} = (K P_i K) mod N P_{i-1} = $Q_i \bigoplus P_i$ end 5. $P = P_0 || Q_0 /* ||$ represents concatenation */ 6. Write (P)

0. ((1)

Let us now see how the functions (1) Mix () and (2) Shift () can be developed.

In the iteration process, we come across a pair of square matrices of size m. Let us suppose that a square matrix of size m denoted by P_i can be written in the form

						٦
	p ₁₁	p ₁₂	p ₁₃		p _{1m}	
	p ₂₁	p ₂₂	p ₂₃		p_{2m}	
$P_i =$	p ₃₁	p ₃₂	р ₃₃	•••••	p _{3m}	(3.1)
		•	•		•	
	•	•	•		•	
	P_{m1}	p_{m2}	p_{m3}	•••••	p_{mm}	

On converting each element of the matrix in its 8 bit binary form we get a matrix of size mx8m.

P111P112P118	P121P122P128P	01m1P1m2P1m8	
p ₂₁₁ p ₂₁₂ p ₂₁₈	p ₂₂₁ p ₂₂₂ p ₂₂₈ p	$p_{2m1}p_{2m2}p_{2m8}$	
p ₃₁₁ p ₃₁₂ p ₃₁₈	p ₃₂₁ p ₃₂₂ p ₃₂₈ p	93m1p3m2p3m8	(3.2)
:	:	:	
:	:	:	
:	:	:	
:	:	:	
$P_{m11}p_{m12}p_{m13}$	$p_{m21}p_{m22}p_{m28}p_{m28}$	$p_{mm1}p_{mm2}\dots p_{mm8}$	

Here each column contains m binary bits. Now to perform the function Shift () on plaintext P_i , we offer a 4 bit down ward circular shift in each column, during the iteration process. This process is known as shifting. Here, it may be noted that the function IShift (), which is the reverse process of Shift () can be readily obtained by giving a 4 bit upward circular shift in every column of the ciphertext C during the iteration process of decryption.

Let us now consider the function Mix (), consider P_i as the matrix represented in (3.2) obtained during the iteration process. This matrix is of size mx8m, where each row contains 8m binary bits. On concatenating the bit of 1st column to bit of 8th column, we get a decimal number, on concatenating the bit of 9 column to bit 16 column, we get another decimal number and by continuing this process till we exhaust all rows and columns, we get the decimal numbers to be arranged in row wise manner to get square matrix of size m. This is the process involved in the function Mix (). Thus we have the new plaintext obtained after the function Mix(). IMix () is the reverse process of Mix () which is used during the process of decryption.

2. Illustration of the Cipher Consider the plaintext given below.

India is a country well known for its great culture, literature etc. Ramakrishna paramahamsa, Vivekananda, Gandhi, these were the great prople. Geetha in Mahabharata is a very great epic. Though it was well known in the past, today India is having crores of liquor shops. Each politician is supporting liquor business. Even the government is getting crores in the form of central exercise tax. I have really been in the country and I have visited every corner. Today, nothing is great about India. One party is fighting with the other. All people are greatly in respect of power. I do not know how Jesus will save them. (4.1)

Let us focus our attention on the first 128 characters of the plaintext. This can be seen as

India is a country well known for its great culture, literature etc. Ramakrishna paramahamsa, Vivekananda, Gandhi, these were th (4.2)

and

On converting each character of the plaintext in (4.2) into its equivalent EBCIDIC code, we get a plaintext matrix P of size 8x16.

 73
 110
 100
 105
 97
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 105
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118 101 107 97 110 97 110 100 97 44 32 71 97 110 100 104

 105
 44
 32
 116
 104
 101
 115
 101
 32
 119
 101

 114
 101
 32
 116
 104
 101
 115
 101
 32
 119
 101

(4.3)

Now from (3.3), consider the left halve as a matrix represented by P_0 , and the right halve as a matrix represented by Q_0 . Thus we have P_0 and Q_0 as

73	110	100	105	97	32	105	115	
114	121	32	119	101	108	108	32	
114	32	105	116	115	32	103	114	
117	114	101	44	32	108	105	116	
101	116	99	46	32	82	97	109	
32	112	97	114	97	109	97	104	
118	101	107	97	110	97	110	100	
105	44	32	116	104	101	115	101	
					(4	.4)		

 $P_0 \!=\!$

Let us take a key matrix denoted by A of size 4x4 as

A =

Γ	69	124	27	167
	135	79	(4	.6)
	248	199	209	75
	239	45	255	92

On using the relations (2.5) to (2.7) and taking d =99, we get the involutory matrix of key matrix A as K, whose size is 8x8. Thus we have the key K as

	-								
-0	69	124	27	167	180	12	143	107	
	135	79	99	111	203	214	183	19	
	248	199	209	75	24	11	144	255	
K=	239	45	255	92	147	153	99	207	
	130	84	233	237	187	132	229	89	
	141	112	1	133	121	177	157	145	
	168	77	134	249	8	57	47	181	
	5	47	181	63	17	211	1	164	
					(4.7)	10			

On using (4.4), (4.5), (4.7) and the functions Shift () and Mix (), we adopt the encryption algorithm given in section 3 and obtain the ciphertext C as

28 188 242 196 4 152 196 240 246 144 220	38 238 178 202 248 222 182 86 188 222 116
218 18 68 132 224	122 156 166 178 236
58 110 90 220 182 222 22 146 102 108 30 8	= 16 146 104 90 188 164 136 6 186 108 152
44 84 154 100	44 170 126 252 64
200 58 122 230 136 10 48 140 172 236 106	196 88 182 248 242 28 228 146 50 2 204
176 182 172 138 74	220 152 212 174 166
140 230 146 62 190 54 42 54 210 230 44	64 212 198 48 204 138 186 28 204 190 12
254 210 88 170 52	156 150 60 48 16
36 176 86 104 144 118 246 206 16 22 98 18	216 58 124 200 88 114 82 86 138 114 218
194 218 70 114	122 98 72 224 236
110 94 150 150 48 236 164 108 6 206 70	244 184 58 120 14 212 176 146 182 142
114 96 194 166 120	58 108 102 56 44 144
182 216 250 66 4 56 202 118 184 38 248	24 52 8 36 150 172 204 224 222 220 242
110 168 182 100 138	70 210 88 184 20
122 206 126 250 150 62 124 54 110 102 100 124 152 128 122 186 (4.8)	176 190 138 48 140 170 114 110 164 98 234 214 146 190 120 202

On applying the decryption algorithm given in section 3 and by using the inputs (4.7), (4.8), along with the functions IShift () and IMix (), we get back the original plaintext given in (4.3).

Let us now examine the avalanche effect which indicates the strength of the cipher in a qualitative manner. To carry out this one, we first consider a one bit change in the plaintext (4.3), this can be done by changing the first row first column element in (4.3) from 73 to 72. By applying the encryption algorithm given in section 3, on the modified plaintext and by keeping the key in (4.7) as it is, we get the cipher text as

76 146 182 142 224 222 220 242 110 164 98 234 (4.9)Now on comparing (4.8) and (4.9) in their binary form, we notice that they differ by 518 bits out of 1024 bits. This shows that the cipher has good strength.

Now let us consider a one bit change in the key. This can be carried out by converting the first row first column element of (4.7) from 69 to 70. On adopting the encryption algorithm given in section 3 along with the modified key, and by keeping the plaintext in (4.3) as it is, we get the ciphertext as

. . .

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120 122 110 0 218 122 222 16 22 72 238 72 98 248 58 104
240 44 58 150 218 226 236 176 36 36 102 152 6 110 76 98
216 218 206 90 254 140 230 146 62 190 170 102 250 86 44 34
114 42 204 136 10 48 140 164 150 168 144 118 246 206 246 180
16 52 152 86 76 242 200 58 120 88 140 36 140 58 198 114

96 194 192 108 240 16 126 108 84 208 220 218 224 236 182 206

60 156 148 246 8 72 172 64 60 222 44 222 210 230 118 216 228 246 254 166 216 146 234 146 126 150 44 248 206 222 40 104

(4.10)

C=

On comparing (4.8) and (4.10) in their binary form we notice that they differ by 504 bits out of 1024 bits. This also shows that the strength of the cipher is quite considerable one.

3. Cryptanalysis

In the study of cryptography, the different cryptanalytic attacks seen in the literature [10] are

1. Cipher text only (Brute Force) attack.

- 2. Known Plaintext attack.
- 3. Chosen Plaintext attack.
- 4. Chosen Cipher text attack.

In all these cryptanalytic attacks, the ciphertext and the encryption are available to the attacker. Generally an encryption algorithm must be designed to withstand the first two attacks [10].

Firstly, let us consider the brute force attack. In this cipher as the key is consisting of sixteen decimal numbers and as each element of the key can be represented as 8 bit EBCIDIC code format, the size of the key is 112 bits. Hence the size of the key space is

$$2^{112} = (2^{10})^{11.2} \approx (10^3)^{11.2} = 10^{33.6}$$

If the time taken to get the plaintext by using one value of the key in the key space is10⁻⁷ seconds, then the time taken to execute the cipher with all possible keys in key space is

 $10^{33.6} \times 10^{-7}$

 $= 3.171 \times 10^{18.6} \text{ years.}$

As this number is very large, it is impractical to break the cipher by using this attack.

Now let us examine the known plaintext attack, to carry out this attack, assume that the attacker knows the plaintext P ciphertext C pairs as many as required.

If we confine our attention to only one round of the iteration process i.e r = 1. Then the relations governing the encryption process for one round can be written as

$\mathbf{P}_1 = (\mathbf{K} \mathbf{Q}_0 \mathbf{K}) \mod \mathbf{N}$	(5.1)
$\mathbf{Q}_1 = \mathbf{P}_0 \qquad \bigoplus \mathbf{P}_1$	(5.2)
$\mathbf{P}_1 = \mathbf{M} \ (\mathbf{P}_1)$	(5.3)
$\mathbf{P}_1 = \mathbf{S} \ (\mathbf{P}_1)$	(5.4)
$\mathbf{Q}_1 = \mathbf{M} \; (\mathbf{Q}_1)$	(5.6)
$\mathbf{Q}_1 = \mathbf{S} \ (\mathbf{Q}_1)$	(5.7)
$\mathbf{C} = \mathbf{P}_1 \ \mathbf{Q}_1$	(5.8)

In known plaintext attack, we know $P_0,\,Q_0$ and C and the encryption algorithm. As the Shift () and Mix () fucntions are known, using (5.8) to

(5.3), we get P_1 and Q_1 occurring on the left hand side of (5.1) and (5.2) As P_0 and the Q_0 occurring on the right hand side of (5.1) and (5.2) are known to the attacker, the key K can not be obtained due to the modulo of N used in (5.1). Thus the cipher cannot be broken by the known plaintext attack even if we confine our attention only to the first round of the iteration process. This shows that it is impossible to break the final cipher obtained after sixteen rounds of the iteration process by using the known plaintext attack.

Intuitively choosing a plaintext or ciphertext and determining the key or a function of the key is a formidable task in the case of this cipher.

Hence from the above discussion we conclude that this cipher is not breakable by all the possible attacks that are available in cryptography.

4. Computations and Conclusions

In this paper, we have investigated the modified Fesitel cipher. In order to introduce confusion and diffusion, we have used a pair of functions namely Shift () and Mix(), and the modulo operation in every round of the iteration. As these features thoroughly mix the plaintext at every stage of the iteration process, the strength of the cipher is good which is proved by the avalanche effect discussed in section 4.

The programs required for encryption and decryption are written in C Language.

In order to encrypt the entire plaintext given in (4.1), the entire plaintext is divided into 5 blocks, with each block containing 128 characters. As the last block contains only 107 characters, we have included 21 blank characters in order to make it a complete block of size 128 characters. On adopting the encryption algorithm given in section 3 with necessary inputs, we get the ciphertext corresponding to the entire plaintext as

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 188
 242
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 4
 152
 196
 240
 246
 144
 220

 218
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 68
 132
 224

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 182
 222
 22
 146
 102
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 30
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200 58 122 230 136 10 48 140 172 236 106 176 182 172 138 74

140 230 146 62 190 54 42 54 210 230 44 254 210 88 170 52

36 176 86 104 144 118 246 206 16 22 98 18 194 218 70 114

110 94 150 150 48 236 164 108 6 206 70 114 96 194 166 120

182 216 250 66 4 56 202 118 184 38 248 110 168 182 100 138

122 206 126 250 150 62 124 54 110 102 100 124 152 128 122 186

- 120 122 104 26 144 86 106 200 16 14 118 118 216 228 246 254
- 118 210 228 240 254

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